## Reg. No:

$\square$

## SIDDHARTH INSTITUTE OF ENGINEERING \& TECHNOLOGY:: PUTTUR (AUTONOMOUS)

B.Tech II Year I Semester Regular \& Supplementary Examinations March-2023 NUMERICAL METHODS, PROBABILITY \&STATISTICS
(Mechanical Engineering)
Time: 3 hours

## (Answer all Five Units $5 \times 12=60$ Marks) <br> UNIT-I

1 Find real root of the equation $3 x=e^{x}$ by Bisection method.
OR
2 From the following table values of x and $y=\tan x$, Interpolate the values of y when CO1 L2 12M $x=0.12$ and $x=0.28$.

| $x$ | 0.10 | 0.15 | 0.20 | 0.25 | 0.30 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $y$ | 0.1003 | 0.1511 | 0.2027 | 0.2553 | 0.3093 |

UNIT-II
3 Solve $y^{1}=x+y$, given $\mathrm{y}(1)=0$ find $\mathrm{y}(1.1)$ and $\mathrm{y}(1.2)$ by Taylor's series method.

4 Evaluate $\int_{0}^{1} \frac{1}{1+x} d x$ by
CO2 L2 12M
(i) Trapezoidal rule and Simpson's $\frac{1}{3}$ rule.
(ii) Using Simpson's $\frac{3}{8}$ rule and compare the result with actual value.

## UNIT-III

5 a State and prove Addition theorem of probability
CO3 L1 6M
b In a certain town $40 \%$ have brown hair, $25 \%$ have brown eyes and $15 \%$ have
CO3 L2 6M both brown hair and brown eyes. A person is selected at random from the town.
i) If he has brown hair, what is the probability that he has brown eyes also?
ii) If he has brown eyes, determine the probability, that he does not have brown hair?

## OR

6 a State Baye's theorem.
CO3 L1 2M
b
Determine (i) $P(B / A)$ (ii) $P\left(A / B^{C}\right)$ if A and B are events with $P(A)=\frac{1}{3} P(B)=\frac{1}{4}$, CO3 L2 10M $P(A U B)=\frac{1}{2}$.

## UNIT-IV

7 A random variable X has the following probability function.

| X | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{P}(\mathrm{X})$ | 0 | K | 2 K | 2 K | 3 K | $\mathrm{~K}^{2}$ | $2 \mathrm{~K}^{2}$ | $7 \mathrm{~K}^{2}+\mathrm{K}$ |

Determine (i) K (ii) Mean iii) variance
(iv) if $\mathrm{P}(\mathrm{X} \leq \mathrm{K})>1 / 2$, find the Minimum value of K

8 For the continuous probability function $f(x)=\left\{\begin{array}{c}k x^{2} e^{-x} \text { when } x \geq 0 \\ 0 ; \text { elsewhere }\end{array}\right.$
CO4 L3 12M

Find i) $k$ ii) Mean iii) Variance

## UNIT-V

9 a If $2 \%$ of light bulbs are defective. Find the probability that
(i) At least one is defective (ii) $P(1<x<8)$ in a sample of 100 .
b If for a Poisson variate $2 \mathrm{P}(\mathrm{X}=0)=\mathrm{P}(\mathrm{X}=2)$ Find the probability that

CO5 L3 6M

CO5 L3 6M

CO5 L3 12M

| X | 10 | 15 | 12 | 17 | 13 | 16 | 24 | 14 | 22 | 20 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Y | 30 | 42 | 45 | 46 | 33 | 34 | 40 | 35 | 39 | 38 |

